

Electromagnetic Compatibility Problem Set 1

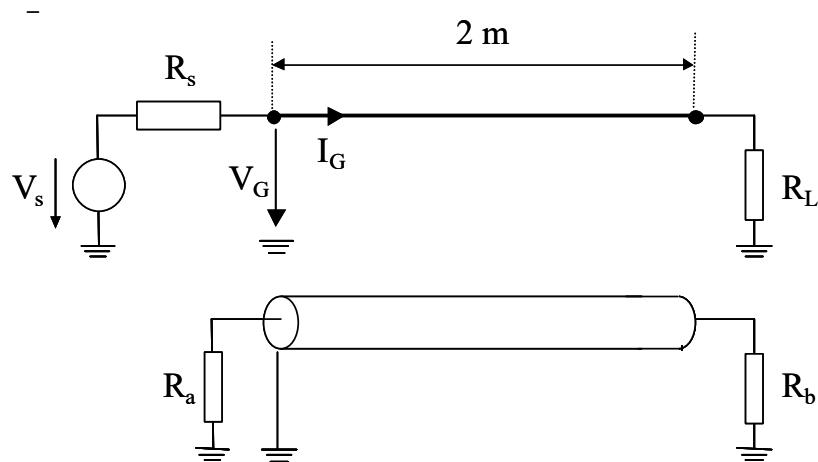
Problem 1

Compute $[Z]$, $[Y]$ and chain matrices associated with the two following circuits.



Problem 2

Consider the following circuit



Line parameters :

$$M = 2 \text{ nH/m}, C_o = 0.6 \text{ pF/m}$$

$$R_s = 0 \Omega, R_L = 50 \Omega, R_a = 100 \Omega, R_b = 200 \Omega$$

$v_s(t)$: sinusoidal excitation with $V_s = 1 \text{ V}$, $f = 1 \text{ MHz}$

A shield is used around the 'receptor' wire, which is connected to the ground plane at one end.

Using the weak coupling approximation :

1. Determine the expressions for the induced voltages V_a and V_b in the frequency domain and in the time domain.
2. Calculate the reduction of the induced voltage in dB.

Problem 3 :

We connect the shield of problem 2 to ground at its two ends. The shield parameters are $R_{sh} = 1 \Omega/\text{m}$ et $L_{sh} = 16 \mu\text{H/m}$,

1. Determine the expression for the induced voltage $V_a(j\omega)$ in the frequency domain.

2. Determine the expression of the induced voltage $v_a(t)$ in the time domain by simplifying the frequency-domain expression.

Problem 4 :

Consider the case of a 10-m long, unbalanced twisted pair with the following parameters:

$R_s = R_L = R_a = R_b = 10 \Omega$. The twist rate is 10 twists/m.

The mutual inductances and capacitances with the disturber line are: $M_1 = 1.641 \times 10^{-7} \text{ H/m}$,

$M_2 = 1.574 \times 10^{-7} \text{ H/m}$ $C_o (\cong C_{o1} \cong C_{o2}) = 1.93 \text{ pF/m}$.

The source in the disturber line is a 5-V, 1-MHz sinusoid.

Assuming the weak coupling approximation, calculate the induced voltages V_a and V_b in the frequency- and time-domain, by separating the inductive and capacitive coupling terms.

Problem 5 : Determination of the transfer impedance of a shielded cable in a triaxial setup

The transfer impedance of a shielded cable can be determined using the so-called triaxial setup (see figure below), in which both transmission lines, the external and the internal, are terminated in their characteristic impedances Z_{cs} and Z_{ci} respectively.

Calculate the analytical expression of the induced voltage in the inner conductor $V_i(0)$ as a function of the injected current in the shield $I_e(0)$. Determine the expression of the transfer impedance.

